


Problem Solving by  
**Case-Based Reasoning**  
 PART 2

Machine Learning  
 Sommersemester 2009  
 23.06.2009

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 Machine Learning Lab



Trailer



**CBR Noir**  
 (c) David Wilson,  
 University of North Carolina



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Agenda

1. Introduction to CBR **PART 1**
2. Knowledge and Case Representation
3. Similarity
4. Similarity-Based Retrieval
5. Solution Adaptation **PART 2**
6. Learning in Case-Based Reasoning
7. Applications
8. References

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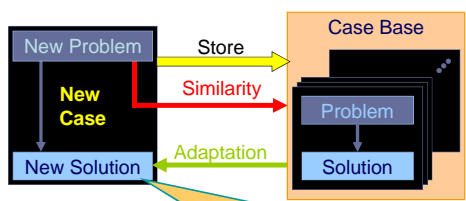
SUMMARY OF PART 1

*What is Case-Based Reasoning?  
 How can cases be represented?  
 When is a new problem (query) similar to a case's problem part?  
 How to retrieve a query's nearest neighbour(s)?*

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Simplified CBR Model

Solve new problems by selecting cases used for similar problems and by (eventually) adapting the belonging solution.



Underlying Assumption: Similar problems have similar solutions!

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A Simple Example Scenario:  
Solving a New Diagnostic Problem

**Case Base with Two Cases**

- each case describes one particular situation
- all cases are independent of one another

<b>Case 1</b>	<b>Problem (Symptoms):</b> - Problem : head light does not work - Car : VW Golf IV, 1.6l - Year : 1998 - Battery Voltage : 13.9V - State of Light : ok - State of Light Switch : ok
	<b>Solution:</b> - Diagnosis : front light fuse defect - Repair : repair front light fuse
<b>Case 2</b>	<b>Problem (Symptoms):</b> - Problem : head light does not work - Car : Audi A4 - Year : 2002 - Battery Voltage : 12.9V - State of Light : surface damaged - State of Light Switch : ok
	<b>Solution:</b> - Diagnosis : bulb defect - Repair : replace front light

**A New Problem (Query) Has to Be Solved**

- we make several observations in the current situation
- observations define a new problem
- not all attribute values have to be known
- Note: The new problem is a "case" without solution part

<b>Problem (Symptoms):</b> - Problem : break light does not work - Car : Audi 80 - Year : 1990 - Battery Voltage : 12.6V - State of Lights : ok - State of Light Switch :
---

**Compare the new problem with each case and select the most similar one!**  
→ **CASE 1**

**Questions:**  
When are two cases similar?  
How to rank the cases according to their similarity?  
How to reuse the solution of the corresponding case?

**Note:**  
Similarity is the most important concept in CBR. Similarity may be assessed based on the similarity of each feature, while the importance of different features may vary (feature weighting).

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### A Simple Example Scenario: Reuse and Retain

- Reuse**
  - adapt the solution
  - how do differences in the problem affect the solution
- Retain**
  - if diagnosis is correct: store new case
  - add case to case base

**Case 1**

**Problem (Symptoms):**

- Problem: front light does not work

**Solution:**

- Diagnosis: front light fuse defect
- Repair: repair front light fuse

**Case 2**

**Problem (Symptoms):**

- Problem: break light does not work
- Car: Audi A80
- Year: 1990
- Battery Voltage: 12.6V
- State of Light: ok
- State of Light Switch: ok

**Solution:**

- Diagnosis: break light fuse defect
- Repair: replace break light fuse

**Case 3**

**Problem (Symptoms):**

- Problem: break light does not work
- Car: Audi A80
- Year: 1990
- Battery Voltage: 12.6V
- State of Light: ok
- State of Light Switch: ok

**Solution:**

- Diagnosis: break light fuse defect
- Repair: replace break light fuse

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### Knowledge Container Model [Richter, 1989]

„In order to solve problems, one needs knowledge.“

- Knowledge of a CBR System**
  - vocabulary: knowledge representation
  - retrieval: similarity assessment (measures)
  - solution transformation: rules
  - cases
- Knowledge Management**
  - as the environment may change, maintenance of the containers' contents over the lifetime of the CBR system is crucial to guarantee its continued usability

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### Similarity

- Similarity is the **central notion** in Case-Based Reasoning.
- Similarity is always considered between problems (not solutions of cases).
- Selection of cases during the "Retrieve" phase is based on the similarity of cases to a given query.

→ **Observation I:** There is no universal similarity; similarity always relates to certain purpose.

→ **Observation II:** Similarity is not necessarily transitive.

→ **Observation III:** Similarity does not have to be symmetric.

- Purpose of Similarity: Selection of solutions that can be easily transferred / adapted to the problem at hand.
- Similarity = Utility for Solving a (new) Problem**
- Goal:** Similarity must approximate utility as accurately as possible.

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### Local-Global Principle

- case description by n attributes  $A_1, \dots, A_n$
- each attribute has a certain type  $T_i$  (e.g. numeric)

- Local Similarity**
  - a separate similarity function is used for each attribute:  $\text{sim}_{A_i}: T_i \times T_i \rightarrow [0, 1]$
  - local measures are depending on the respective type  $T_i$  of the attribute  $A_i$
- Global Similarity**
  - Very frequently used in practice!
  - $\text{sim}(x, y) = \text{sim}((x_1, \dots, x_n), (y_1, \dots, y_n)) = F(\text{sim}_{A_1}(x_1, y_1), \dots, \text{sim}_{A_n}(x_n, y_n))$
  - $F: [0, 1]^n \rightarrow [0, 1]$  → **Amalgamation Function**
  - requirements on F:
    - F is monotonous in each of its arguments
    - $F(0, \dots, 0) = 0$  and  $F(1, \dots, 1) = 1$

**Examples:**

- Weighted Average  $F(s_1, \dots, s_n) = \sum_{i=1}^n w_i s_i$
- Maximum  $F(s_1, \dots, s_n) = \max(s_1, \dots, s_n)$
- k-Minimum  $F(s_1, \dots, s_n) = s_k$  with  $s_1 \leq s_2 \leq \dots \leq s_n$
- etc.

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### Local Similarity Measures

(for unordered symbolic and integer/real-valued attribute types)

#### Similarity Tables

- for attributes with symbolic type  $T_A = \{v_1, \dots, v_k\}$
- $\text{sim}_A(x, y) = s[x, y]$
- example: attribute "RAM-Type" with  $T_A = \{\text{SD, DDR, RD}\}$

q \ c	SD	DDR	RD
SD	1.0	0.9	0.75
DDR	0.5	1.0	0.75
RD	0.25	0.5	1.0

RAM-Type

- reflexive similarity measure: diagonal elements  $s[k, k] = 1$
- symmetric similarity measure:  $s = s^T$

#### Difference-Based Similarity Functions

- for attributes with numeric type (e.g. integer or real-valued)
- similarity is based on the numerical difference between case and query value
  - linearly scaled domains:  $\text{sim}_A(x, y) = f(x - y)$
  - exponentially scaled domains:  $\text{sim}_A(x, y) = f(\log(x) - \log(y))$
- examples:
  - asymmetric
  - query depends on maximum value of attribute
  - asymmetric
  - e.g. maximum price of a car is a requirement
  - background knowledge: minimum price required by a customer

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### Case Retrieval Approaches

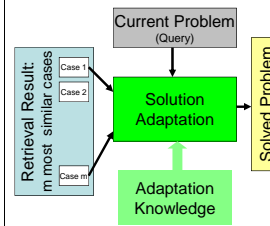
- Retrieval Task**
  - Input
    - case base  $CB = \{c_1, \dots, c_n\}$
    - similarity measure  $\text{sim}$
    - query (new problem)  $q$
  - Output
    - most similar case  $c_i$
    - or
    - m most similar cases  $\{c_1, \dots, c_m\}$
    - or
    - all cases  $\{c_1, \dots, c_n\}$  which have at least a similarity of  $\text{sim}_{\min}$  to  $q$
  - Main Problem: Efficiency
  - Question: How can the case base be organised in such a way to support an efficient retrieval?
- Sequential Retrieval**
  - iterates over all  $c \in CB$  and calculates  $\text{sim}(c, q)$
- Two-Stage Retrieval**
  - MAC/FAC approach
- kd-Tree Retrieval**
  - builds up index structure

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## 5. SOLUTION ADAPTATION

*How to adapt existing solutions to be applicable for the problem at hand?*

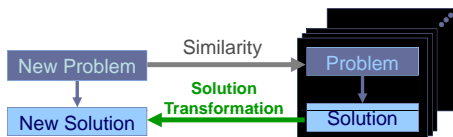
## Overview on Solution Adaptation



- Types of Adaptation
  - null adaptation
  - transformational analogy (transformation-based)
  - generative adaptation (derivational analogy)
  - compositional adaptation → combine several cases' solutions to gain a solution to the new problem
  - hierarchical adaptation

## Transformational Analogy

- **Idea:** Transform the Solution of a Similar Problem



- Representation of Adaptation Knowledge
  - by a fixed set of adaptation rules
  - by a fixed set of adaptation operators
- Types of Transformations
  - **substitutional:** change, insert, remove of parts of the solution or parameters
  - **structural:** reorganisation of the solution, insertion or deletion of objects

## Example: Adaptation Rules for Transformational Analogy

- Product Recommendation System for PCs
  - CBR system with case base of pre-configured PC systems
  - user specifies inquiry / claims
  - system chooses the best PC system and eventually modifies some components appropriately

- Exemplary Rule for Substitutional Adaptation

```
if query.database_applications==true
  and retrieved.diskspace<100GB
then
  target.diskspace:=160GB
```

- Exemplary Rule for Structural Adaptation

```
if query.games==true
  and retrieved.games==false
then
  addObject target.gamecontroller
  addObject target.soundcard
```

## Generative Solution Adaptation

- Assumption: **Availability of a (knowledge-based) Problem Solver**
  - capable of solving any problem without cases
  - i.e. comprising sufficient domain knowledge
  - disposing of an inference mechanism
- Why use cases at all?
  - to find the solution faster
  - to find a solution similar to existing solutions
  - to obtain a solution by adapting an existing solution as little as possible
- Derivational Analogy (most prominent form of GSA)
  - Case = Problem + Solution + Inference (path to the solution)
  - Idea
    - reuse parts of the path to the solution for the current problem
    - combine (eventually) solution paths from several cases
    - solve the remaining gaps in the solution by using the generative problem solver
  - Algorithmic Realisations: One-Shot Replay and Interleaved Replay

## Comparison of Transformation-Based and Generative Adaptation

### Generative Adaptation

- explicit problem-solving knowledge is necessary
- cases must contain the steps towards the solution (solution path)
- if problem-solving knowledge is correct, correctness of the final solution is guaranteed
- usually: usage of experience (cases) yields improved efficiency

### Transformation-Based Adaptation

- **no** explicit problem-solving knowledge is necessary
- explicit knowledge about solution adaptation is required
- cases need **not** contain the steps towards the solution
- correctness of the final solution is **not** guaranteed
- usually: usage of experience (cases) yields increased competency (e.g. improvement of classification accuracy)
- Is a rather heuristic/conservative method – much knowledge has to be incorporated (e.g. in order to transform one PC into a very different one).

### Relation between Solution Adaptation and Retrieval

- Possible Purpose of Similarity
  - ➔ Selection of Solutions that are Easily Adaptable to the Current Problem
- Goal:
  - Similarity = Adaptability of the Solution to the New Problem
- Note:
  - Adaptability is an a-posteriori criterion. The adaptability of a problem can usually be assessed only **after** having solved the problem.
  - Similarity regarding the cases' problem parts is an a-priori criterion. Similarity must be determined **before** having solved the problem.
- Goal:
  - Similarity should predict/approximate adaptability as good as possible.
  - Possible solution: Use machine learning to obtain (learn) a similarity measure that explicitly considers the adaptability of cases, too. (cf. next chapter)

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## 6. LEARNING IN CASE-BASED REASONING

*How are other Machine Learning approaches utilized in the context of CBR systems?*

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### Learning and the Retain Phase

- Tasks of Learning in the Retain Phase
  - improvement of competence of the system
  - improving/maintaining the system's efficiency
- Processing of New Experience
  - may imply reorganisation of the case base (rebuilding of index structures)
  - adding new cases to the case base
  - removal of old cases from the case base
  - improvement of similarity assessment
    - ➔ learning similarity measures
  - improvement of solution adaptation

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### Instance-Based Learning

- IBL Algorithms
  - type of case-based learning where only the case base is being adapted (similarity measures remain constant)
  - Here: focus on
    - attribute value-based case representation
    - real-valued attributes
    - classification tasks
- Input
  - some similarity (or distance) measure (e.g. Euclidean distance)
  - sequence  $T=(c_1, \dots, c_n)$  of training cases  $c_1, \dots, c_n$
- Output
  - (final) case base  $CB=CB_n$
- Variants
  - IB1: addition of each case to the case base
  - IB2: addition of case  $c$  if it is being classified wrongly by the current case base
  - IB3: addition of case  $c$  if it is being classified wrongly by the current case base and removal of "bad" cases

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### IB1 and IB2

- IB1
 

```
CB := {}
for i:=1 to n do
  CB := CB ∪ {ci}
```

  - Problem: Case base may be growing extremely. If IB1 was used in the CBR cycle's retain phase, a case would be added to the case base after each problem-solving.
- IB2
 

```
CB := {}
for i:=1 to n do
  ci := (pi, si) //p=problem, s=class
  retrieve nearest neighbour c'=(p', s') of c as
  c' := argmaxc'∈CB sim(ci, c)
  if si ≠ s' //misclassification
  then CB := CB ∪ {ci}
```

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### Remarks on IB2

- Properties
  - IB2 is dependent on the sequence of presentation of the cases
    - ➔ Even though a training case  $c$  might be classified correctly during the training (and for that reason is not added to the case base), it may happen that  $c$  will be classified wrongly by the final case base  $CB_n$ .
  - IB2 stores much less cases than IB1.
  - Empirically: IB2 yields only slightly worse classification accuracies than IB1.
- Drawbacks
  - difficulties in handling noisy data
    - ➔ noisy data points are (usually) classified incorrectly
    - ➔ hence, they are added to the case base
    - ➔ overall classification accuracy decreases
  - Goal: IB3 ought to be capable of handling noisy data.
    - ➔ Extension introduced in IB3: For each case  $c$  a statistic concerning the classification accuracy  $CA(c)$  is maintained.

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## IB3 (I)

### Algorithm IB3

$$CA(c) = \frac{\text{number of instances classified correctly with } c}{\text{number of instances classified in total with } c}$$

```

CB := {}
for i:=1 to n do
  ci := (pi, si) //p=problem, s=class
  CBacc := { c ∈ CB | acceptable(c) }
  if CBacc != {}
  then
    c' := argmaxc ∈ CB sim(c, c) with c'=(p', s')
  else
    j := random number from {1,...,|CB|}
    c' := case from CB that has the j-highest similarity to ci
  if si != s' then //we have a wrong classification
    CB := CB ∪ {ci}
  for all c'=(p', s') ∈ CB with sim(pi, p') >= sim(pi, p') do
    update statistic CA(c') w.r.t. si and s'
    //correct classification (si=s') → increment numerator and denominator of CA(c')
    //wrong classification (si≠s') → increment denominator of CA(c') only
    if significantlyBad(c') then
      CB := CB \ {c'}
  
```



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## IB3 (II)

- different statistical measures are usable to implement the predicates concerning the classification accuracy
- simple variant
  - acceptable(c) iff.  $CA(c) > \theta_1$
  - significantlyBad(c) iff.  $CA(c) < \theta_2$
- $\theta_1$  and  $\theta_2$  are parameters to control the algorithm



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## Remarks on IBx

- Discussion of IB3
  - strong sensitivity to irrelevant features
    - storage requirements scale exponentially with the number of irrelevant features
  - higher classification accuracies and lower storage requirements than IB1 and IB2
- Extension to IB4: Tolerating Attributes with Uncertain Relevance [for details, see Aha, 1992]
  - feature-specific weights used in the similarity computation
  - weights are adjusted using a simple performance feedback algorithm (weight learning) to reflect the relevance of the attributes used to describe the training instances
  - storage requirements are nearly constant with respect to the number of irrelevant features



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## Formal Considerations

- There are numerous formal analyses of IBx algorithms.
  - Here: Focus on convergence proof of IB1 for the two-dimensional case ( $D=[0,1] \times [0,1]$ ).
- Goal:** How many training instances are needed for IB1, to obtain with high probability ( $1-\gamma$ ) a nearly correct ( $\epsilon$ -correct) characterisation of the searched concept.
  - Definition:** Let  $X \subseteq \mathbb{R} \times \mathbb{R}$ ,  $P$  a probability distribution on  $X$ , and  $\epsilon > 0, \gamma > 0$ . A subset  $S \subseteq X$  is a  $(\epsilon, \gamma)$ -Net for  $X$  iff. there is an exception set  $Y \subseteq X$  with
    - $P(Y) \leq \gamma$
    - $\forall x \in X \setminus Y \exists s \in S$  with  $|x-s| < \epsilon$



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## Coverage Lemma

- Idea: Show that a sufficiently large subset  $S$  from  $[0,1] \times [0,1]$  is with "high" probability a  $(\epsilon, \gamma)$ -Net.
- Lemma:** Let  $X=[0,1] \times [0,1]$  and  $\epsilon, \gamma, \delta \in (0,1)$ . Then, there is a  $n_0 > 0$  so that it holds for each  $S \subseteq X$  with  $|S|=n > n_0$ :
 
$$P(S \text{ is an } (\epsilon, \gamma)\text{-Net}) \geq 1 - \delta$$
- Interpretation:** If we are in possession of many cases (more than  $n_0$ ), then we have with high probability ( $\geq 1-\delta$ ) a classifier, for which there is with high probability ( $\geq 1-\gamma$ ) for each problem a case with very small distance ( $< \epsilon$ ) in the case base.
- Extension to  $m$  Dimensions
  - number of necessary instances grows exponentially with the number of attributes

$$n_0 = \frac{(\frac{\sqrt{m}}{\epsilon})^m}{\gamma} \cdot \ln \frac{(\frac{\sqrt{m}}{\epsilon})^m}{\delta}$$



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## Convergence Theorem (I)

- Proof (of Coverage Lemma):** see Blackboard
  - It can be shown that  $n_0 = (k^2/\gamma) \ln(k^2/\delta)$
- Note
  - So far, only statement on the density by which the problem space is covered.
  - So far, no statement on the learned concepts.
- Definition:** Let  $C \subseteq \mathbb{R} \times \mathbb{R}$ . The  $\epsilon$ -Kernel of  $C$  is defined as  $K_\epsilon(C) = \{ x \in C \mid \text{for all } y \in \mathbb{R} \times \mathbb{R} \text{ with } |x-y| < \epsilon \text{ it holds } y \in C \}$ .
- Definition:** Let  $C \subseteq \mathbb{R} \times \mathbb{R}$ . The  $\epsilon$ -Environment of  $C$  is defined as  $U_\epsilon(C) = \{ x \in \mathbb{R} \times \mathbb{R} \mid \text{there is a } y \in C \text{ with } |x-y| < \epsilon \}$ .



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### Convergence Theorem (II)

- Definition:** Let  $C \subseteq \mathcal{X} \times \mathcal{Y}$ ,  $\varepsilon > 0$ ,  $\gamma > 0$ ,  $P$  be a probability distribution on  $\mathcal{X} \times \mathcal{Y}$ . Then,  $C' \subseteq \mathcal{X} \times \mathcal{Y}$  is called an  **$(\varepsilon, \gamma)$ -Approximation** of  $C$  iff. there is an exception set  $Y \subseteq \mathcal{X} \times \mathcal{Y}$  with
  - $P(Y) \leq \gamma$
  - $K_\varepsilon(C) \setminus Y \subseteq C' \setminus Y \subseteq U_\varepsilon(C) \setminus Y$
- Visualisation

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### Convergence Theorem (III)

- Idea: Show, that IB1 approximates a searched target concept  $C$  by  $C'$  with high probability, if a sufficient amount of training cases is available.
- Theorem:** Let  $\varepsilon, \gamma, \delta \in (0, 1)$ ,  $C \subseteq \mathcal{X} \times \mathcal{Y}$  be a bounded set,  $T$  a set of training cases and  $n_0$  given as determined by the Coverage Lemma. It holds: If  $T > n_0$ , then the concept determined by the IB1 algorithm, is an  $(\varepsilon, \gamma)$ -Approximation of  $C$  with probability  $p > 1 - \delta$ .
- Remarks
  - IB1 always converges to a correct classifier, given a sufficient number of training data.
  - If the  $\varepsilon$ -kernel is empty, the concept learnt may be empty, too.
  - The smaller the concept to be learnt, the worse the classification accuracy may become.

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### Learning Attribute Weights

- Goal:** Improving the Similarity Assessment by Adapting the Feature Weights
- Weight Models:
  - global weights:  $\text{sim}(q, c) = \sum w_i \text{sim}(q_i, c_i)$
  - local weights (class-specific weights):  $\text{sim}(q, c) = \sum_{w_i(\text{class}(c))} w_i \text{sim}(q_i, c_i)$  ( $w_i$  as relevance matrix)
  - case-specific weights:  $\text{sim}(q, c) = \sum w_{ic} \text{sim}(q_i, c_i)$
- Weight Adaptation
  - changing the relevance of certain features for the solution
  - numerous learning approaches exist
  - learning **with or without feedback** provided by retrieval/reuse
    - without: exploitation of the distribution of the cases in the case base to determine the relevance of features
    - with: correct / incorrect case selection or classification result implies an adaptation of the weights (e.g. IB4)

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### Learning Local Similarity Measures

- Remember: Local vs. Global Similarity Measures
  - compare query and case values of single attributes
$$\text{Sim}(Q, C) = \sum_{i=1}^n w_i \cdot \text{sim}_i(q_i, c_i)$$
- Similarity Measures: Heuristics to select **useful** cases
  - traditional approach:** Knowledge-Poor Similarity Measures
    - e.g. Hamming Distance
    - mainly based on syntactical differences
    - consider no or only little domain knowledge
    - + easy to define
    - lead often to poor retrieval results
  - alternative approach:** Knowledge-Intensive Similarity Measures
    - e.g. use of sophisticated **local similarity measures**
    - based on knowledge about influences on the utility of cases
    - + better retrieval results
    - require deeper analysis of the domain and more modelling effort

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### Local Similarity Measures (rep.)

- Representation Depends on Attribute Type
  - numeric:** difference-based similarity function
  - symbolic:** similarity table

q \ c	ROM	RW	DVD
ROM	1.0	1.0	0.9
RW	0.0	1.0	0.3
DVD	0.0	0.3	1.0

**CD-Drive**  
encodes knowledge about the functionality of CD-Drives

**Problems:**

- modelling of local similarity measures is costly
- necessary domain knowledge is usually difficult to acquire

➔ **Idea:** Application of Machine Learning techniques

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### Learning Similarity Measures from Utility Feedback

**Teacher** (User / Expert / Evaluation-Function) provides feedback to the CBR-System.

The CBR-System uses a **Query** to determine a **Similarity Measure** from the **Case Base**.

The **Similarity Measure** determines the **Retrieval Result** (Cases 1-8).

The **Retrieval Result** is evaluated against a **Utility** function (Training Example) to calculate a **Retrieval Error E**.

The error is **caused by** the similarity measure.

**Goal:** Finding a similarity measure that minimises  $E$

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## Evolutionary Similarity Measure Optimisation

- Evolutionary Algorithms
  - search algorithms based on the mechanics of natural genetics, selection, and the principle "survival of the fittest"
  - reproduction via crossover and mutation of individuals
  - differentiation from (standard) genetic algorithms
    - representation of individuals (example)
 

```
GA 0 1 1 0 1 0 0 0 1 1 0 0 1 1 1 1 0 ...
EA 0.3 1.3 2.6 -0.11 4 0.7 4.1 7.6 -2.34 0 0.0 0.1 -0.78 3 2.4 6.2 0.1 ...
```
    - specialised genetic operators
- Advantages
  - robust and powerful search strategy
  - ability to handle complex entities such as local similarity measures
  - adequate representation of local measures as individuals

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## Representing Individual

- Similarity Functions per Sampling
 

"Target" Similarity Measure

Sampling (s=7)

Representation as Individual

index	sim value
1	1.0
2	1.0
3	1.0
4	1.0
5	0.2
6	0.05
7	0.0
- Similarity Tables as Matrices
 

q \ c	SD	DDR	RD
SD	1.0	0.9	0.75
DDR	0.5	1.0	0.75
RD	0.25	0.5	1.0

RAM-Type

similarity table individual represented as matrix

1.0	0.9	0.75
0.5	1.0	0.75
0.25	0.5	1.0

Approximated Similarity Measure

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## Specialised Genetic Operators & Evaluation

[for details, see Stahl & Gabel, 2006]

- Several Specialized Operators Implemented
  - simple mutation
  - in-/decreasing mutation
  - simple crossover
  - arithmetical crossover
  - line/row crossover
- Standard Control Algorithms of the EA
  - specialty: simultaneous learning of several local similarity measures is possible via **round robin optimisation**
- Experimental Evaluation
  - learn a similarity measure that considers provided **case adaptation possibilities** during case retrieval
  - Scenario: product recommendation system for PCs with **adaptation rules** for customisation
  - Results: retrieval quality improved by approximately 50%

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## Specialised Genetic Operators

Exemplary Operators:

- simple mutation

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## Specialised Genetic Operators

Exemplary Operators:

- simple mutation
- in-/decreasing mutation

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## Specialised Genetic Operators

Exemplary Operators:

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## Specialised Genetic Operators

**Exemplary Operators:**

- simple mutation
- in-/decreasing mutation
- simple crossover
- **arithmetical crossover**

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## Specialised Genetic Operators

**Exemplary Operators:**

- simple mutation
- in-/decreasing mutation
- simple crossover
- arithmetical crossover
- **line/row crossover**

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## Control Algorithm

**SELECTION**

1. add  $P_n$  to  $P$
2. increase age
3. remove dead/unfit individuals

**BREEDING**

1. choose mating partners
2.  $P_n$  := set of individuals created by crossover/mutation

**EVALUATION**

1. assign **fitness** value
2. assign lifetime value

1. translation: individual to similarity measure  
2. export sim measure  
3. retrieval  
4. error calculation

- simultaneous learning of several local similarity measures: **round robin optimisation**

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## Experimental Evaluation (I)

- Idea: learn a similarity measure that considers provided case adaptation possibilities during case retrieval
- Scenario: product recommendation system for PCs with **adaptation rules** for customisation
- Example:

**Semantic 1:**  
Utility with respect to performance

q \ c	SD	DDR	RD
SD	1.0	0.9	0.75
DDR	0.5	1.0	0.75
RD	0.25	0.5	1.0

RAM-Type

➔

**Semantic 2:**  
Utility with respect to performance but under consideration of possibilities to **adapt cases**

q \ c	SD	DDR	RD
SD	1.0	<b>1.0</b>	0.75
DDR	<b>1.0</b>	1.0	0.75
RD	0.25	0.5	1.0

RAM-Type

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## Experimental Evaluation (II)

- Automated Creation of Training Examples

**Measuring Learning Results**

- CR1
- CR3

optimal case:  $C_3$  ?  
learned measure retrieves:  $C_1, C_2, C_3$

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## Experimental Evaluation (III)

### Dependency on Training Data Size

#Training Examples	CR3avg (%)	CR1avg (%)
0	54.3	29.3
10	64.2	35.4
200	75.3	47.8

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## Discussion

- Learning Knowledge-Intensive Local Similarity Measures
  - simplified definition of accurate similarity measures
  - overcome the problems of knowledge acquisition
  - better approximation of the underlying utility function
- Necessary Precondition
  - sufficient amount of easily acquirable training data

## 7. APPLICATIONS AND TOOLS

*Is CBR actually employed in practice?  
Are there tools available I may use for trying out some  
of the things introduced in this talk?*

## Typical Applications ...

- ... are to be found (among others!) in the areas of
  - medicine (medical diagnosis)
  - law (textual case-based reasoning)
  - banking (credit-risk assignment)
  - engineering, engine-construction, plant construction (gas turbines)
  - biology and environment protection (waste-water treatment)
  - e-commerce (product recommendation, configuration)
- Demonstration video on ...
  - imitating a RoboCup soccer player using case-based reasoning.
  - description of how the imitating agent learns through observation and of how it imitates
  - behavior of the imitating agents at different stages of the learning process



## e-Commerce

- Numerous Applications with Focus on Retrieval and/or Configuration
- WebSell Project for Online Shops
  - Case-Based Retrieval (and Collaborative Recommendation / Customization)
    - tourism
      - Check Out Touristik ([www.reiseboerse.com](http://www.reiseboerse.com))
      - Müritz Online ([www.muertiz.de](http://www.muertiz.de))
    - residential letting
      - Hooke & MacDonald ([www.hookemacdonald.com](http://www.hookemacdonald.com))
    - used cars
      - Quoka ([www.autoaktuell.de](http://www.autoaktuell.de))
    - search in online warehouses
      - Shopping24 ([www.shopping24.de](http://www.shopping24.de))
    - online shopping
      - special switches ([www.jola-info.de](http://www.jola-info.de))
      - music ([www.intercox.de](http://www.intercox.de))
      - general ([www.otto.de](http://www.otto.de))
    - product advisor
      - plastics products ([www.plastics.bayer.com](http://www.plastics.bayer.com))
      - white products ([www.neck.nl](http://www.neck.nl))
    - after sales support
      - Software AG knowledge center ([www.sag.de](http://www.sag.de))



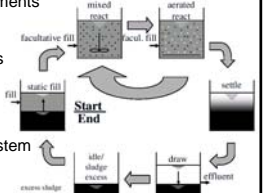
## Diagnosis of Gas Turbines

- application at General Electrics (Atlanta)
- Goal: CBR-based diagnosis of faults
- System Specifics
  - time series of sensor values read from some time prior to failure
  - higher-level representation via knowledge-based feature extraction
  - CBR system is configured via XML files (plug and play)
    - similarity measures, weights, specific case bases to be used
  - retrieve: number of nearest neighbours from selected case base
  - weighted voting to decide for one particular diagnosis (single answer)
  - recommendation provided by the system is enhanced by a confidence level statement
    - for more details see: [Devaney & Cheetham, 2005]



## Waste-Water Treatment

- Sequencing Batch Reactor Plants
  - no continuous inflow of treatment chemicals
  - treatment processes in one single reactor
  - cyclic treatment procedure (cycle duration is 3-8h)
- Treatment in Practice
  - much habitual knowledge applied by the plant inspector
    - often applying sub-optimal treatments
  - case-knowledge is intuitive and self-explaining
    - easier to overcome "bad" habits
- Zerberus Project
  - preliminary stage: case collection by questionnaires
  - 70 actual cases, online retrieval system
  - applied in Rhineland-Palatinate
    - [www.zerberus-online.de](http://www.zerberus-online.de)

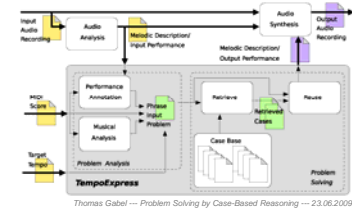


## Expressivity-Preserving Music Transformations

- expressivity-aware tempo transformations of monophonic audio recordings (saxophone jazz)
- rendering at another tempo, while preserving naturally sounding expressivity
- CBR-based approach: TempoExpress

– audio examples

- [original](#)
- [uniform transform](#)
- [CBR-based transformation](#)



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## CBR in the Health Sciences

- CBR is frequently used for medical diagnosis and support
  - diabetes treatment
    - real-time monitoring of glucose level
    - insuline dosage planning using CBR
  - dialysis medicine
  - cancer treatment
    - dose planning in radiotherapy
    - deriving treatment plans including adaptation



• References

- [www.cbr-health.org](http://www.cbr-health.org)
- [www.cbr-biomed.org](http://www.cbr-biomed.org)

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## Poker Playing

- A CBR Approach to Create an Intelligent and Adaptive Poker Player (demo video)



(c) Ian Watson, University of Auckland



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## Other Applications

- Chat/Fun Applications (chatting bots)
  - iGod ([www.titane.ca/concordia/dfar251/igod](http://www.titane.ca/concordia/dfar251/igod))

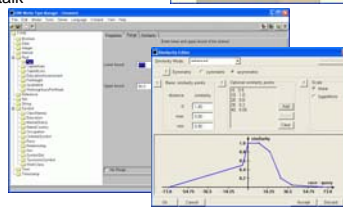


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## Tools

- CBR Works
  - very comprehensive
  - developed as research prototype
  - implemented in Smalltalk
  - applied in many practical applications
- orange
  - commercial product by empolis ([www.empolis.com](http://www.empolis.com))
  - implemented in Java
  - version for students available in use by many large-scale customers (Siemens, Otto, Bayer, etc.)



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## Summary as a Video

- CBR Noir
  - „Sleuthy introduction to case-based reasoning“
  - A Murder Mystery Cycle in Five Parts
  - winner of best video narration award (AAAI 2008)
  - mentions lots of names of CBR tools (for insiders)



(c) David Wilson, University of North Carolina

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## 8. REFERENCES

Where can I find more about CBR?



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## General References

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  - short characterization of CBR  
(in German, <http://www.dki.de/web/km/kompetenz/forschung/fallbasiertes-schliessen>)
  - CBR at Wikipedia: [http://de.wikipedia.org/wiki/Fallbasiertes\\_Schlie%C3%9Fen](http://de.wikipedia.org/wiki/Fallbasiertes_Schlie%C3%9Fen)
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- Articles for Specific Topics
  - Smyth, B., Keane, M. (1995): Remembering to Forget. Proceedings of IJCAI 1995, pages 377f.
  - Wetschereck, D., Aha, D. (1995): *Weighting Features*. Proceedings of ICCBR'95, pages 347-361.
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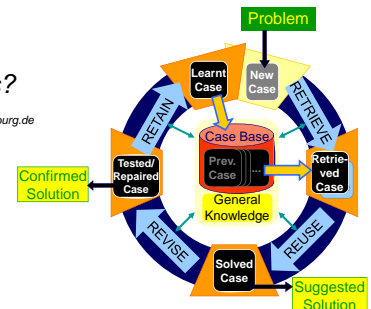


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Thanks!

Questions?

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END